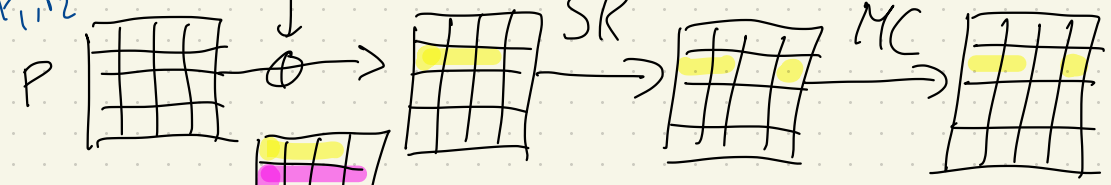


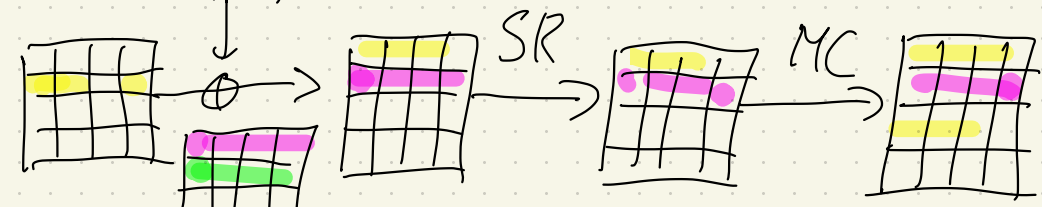

P_1, P_2, \dots, P_e

$h_1 \in \{0, 1\}^{20}, K \in \{0, 1\}^{64}$

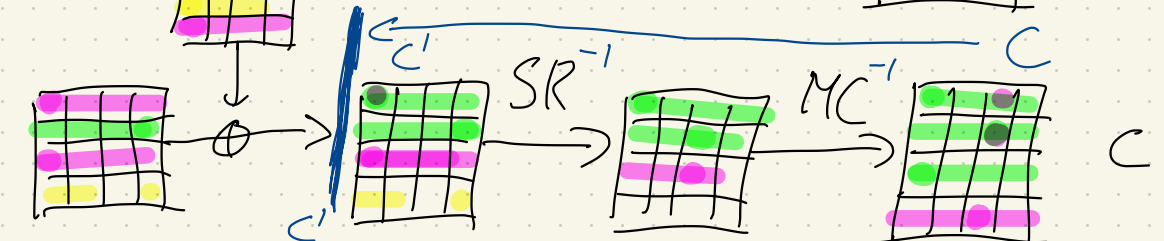
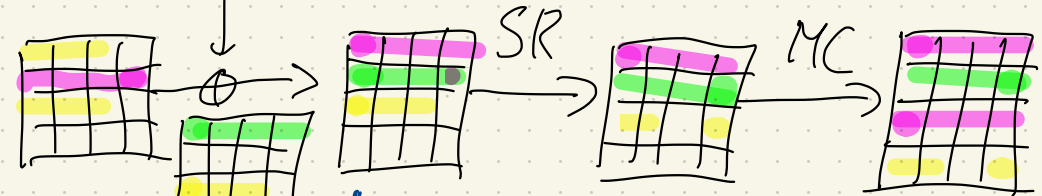
$$M = \begin{pmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \\ 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix}$$

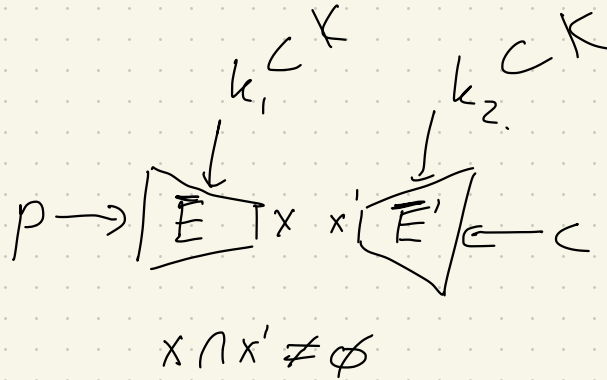
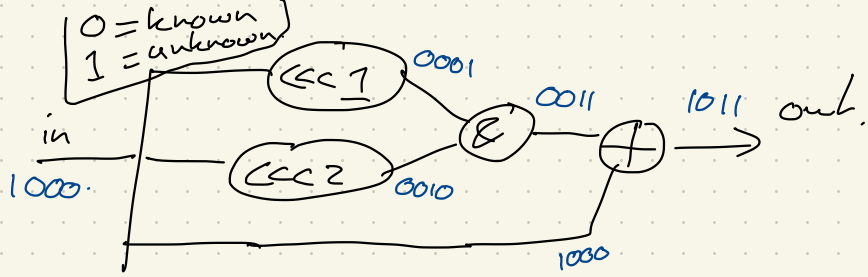
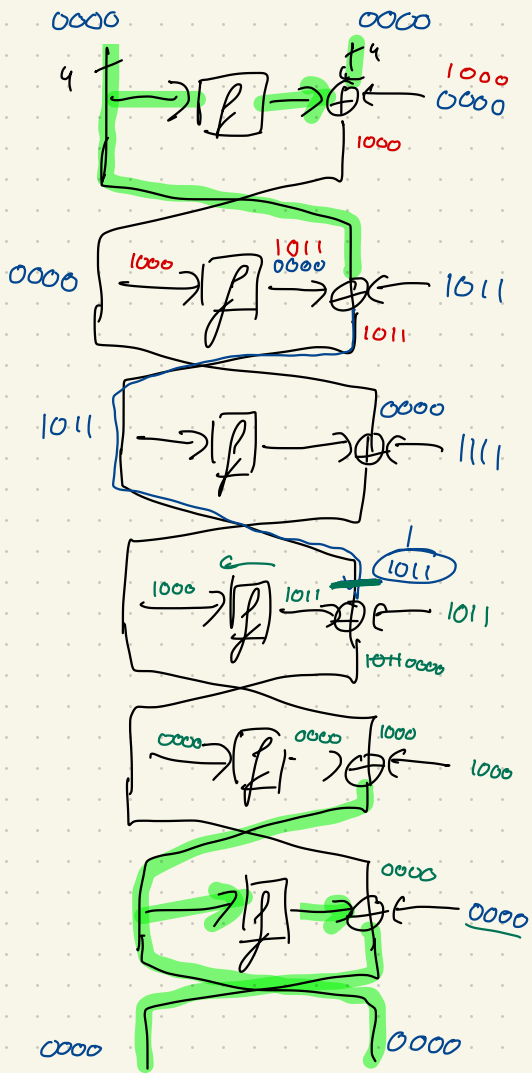


$$\begin{pmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 1 & 0 \\ 1 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{pmatrix} \cdot \begin{pmatrix} a \\ b \\ c \\ d \end{pmatrix} = \begin{pmatrix} a+c \\ b+c \\ a+d \\ c \end{pmatrix}$$



$$M \cdot \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}$$





Phase 1

$H: X \rightarrow k_1$

for $k_1 \in K_1$:

... $x = \{ \}$

... for $p \in P$:

... $x = \{ \bar{E}_{k_1}(p) \}$

... $H[x] \rightarrow k_1$

Phase 2

for $k_2 \in K_2$:

... $x' = \{ \}$

... for $c \in C$:

... $x' = \{ \bar{E}'_{k_2}(c) \}$

... if $x' \in H$:

... output $H[x']$, k_2 prob.